

Chapter 19: Surface Area and Volume of a Right Circular Cylinder

Exercise 19.1

- 1.) Curved surface area of a right circular cylinder is 4.4 m^2 . If the radius of the base of the cylinder is 0.7 m . Find its height.

→ Here, given that

The curved surface area of a right circular cylinder } = 4.4 m^2

Radius of the base of the cylinder = 0.7 m

Let us consider 'h' is the height of a right circular cylinder.

But we know that,

Curved surface area of a cylinder = $2\pi rh$

$$\Rightarrow 4.4 = 2 \times 3.14 \times 0.7 \times h$$

$$\boxed{h = 1 \text{ m}}$$

Thus, the height of given right circular cylinder is found to be 1 m .

- 2.) In a hot water heating system, there is a cylindrical pipe of length 28 m and diameter 5 cm . Find the total radiating surface in the system.

→ Here, given that

Length of the cylindrical pipe } = Height of the cylinder } = $h = 28 \text{ m}$
= 2800 cm

Diameter of the circular end of the cylindrical pipe } = 5 cm

Then, Radius of the circular end of the pipe } = $\frac{5}{2} = 2.5 \text{ cm}$

But, we have

$$\begin{aligned} \text{Curved surface area of cylindrical pipe} &= 2\pi r h \\ &= 2 \times 3.14 \times \frac{5}{2} \times 2800 \\ &= 44000 \text{ cm}^2 \end{aligned}$$

Thus, the area of the radiating surface is found to be 44000 cm^2 .

3.) A cylindrical pillar is 50 cm in diameter & 3.5 m in height. Find the cost of painting the curved surface of the pillar at the rate of Rs. 12.50 per m^2 .

→ Here given that,

The diameter of cylindrical pillar = 50 cm

Then, Radius of cylindrical pillar = $\frac{50}{2} = 25 \text{ cm}$

Height of the cylindrical pillar = $h = 3.5 \text{ m}$

$$\begin{aligned} \text{The curved surface area of cylindrical pillar} &= 2\pi r h \\ &= 2 \times 3.14 \times 0.25 \times 3.5 \\ &= 5.5 \text{ m}^2 \end{aligned}$$

Thus, the total curved surface area of cylindrical pillar is found to be 5.5 m^2 .

The cost of painting curved surface of the pillar is Rs. 12.50 per m^2 .

$$\begin{aligned} \text{Then total cost required for painting the total curved surface area of } 5.5 \text{ m}^2 &= 5.5 \times 12.50 \\ &= 68.75 \end{aligned}$$

Hence, the total cost of painting cylindrical pillar is Rs. 68.75

4.) It is required to make a closed cylindrical tank of height 1m & the base diameter of 140cm from a metal sheet. How many square meters of the sheet are required for the same?

→ Given that, The height of closed cylindrical tank } = h = 1m

Base diameter of cylindrical tank = 140cm

Then, Radius of base of cylindrical tank = $\frac{140}{2} = 70\text{cm}$
= 0.7m

Now,

The area of sheet required to make the cylindrical tank is nothing but the total surface area of tank.

$$\begin{aligned}\text{Total Surface area of tank} &= 2\pi r(h+r) \\ &= 2 \times 3.14 \times 0.7 (1+0.7) \\ &= 7.48 \text{ m}^2\end{aligned}$$

→ Thus, 7.48 m² metal sheet is needed to make the required cylindrical tank.

5.) A solid cylinder has a total surface area of 462 cm². Its curved surface area is one-third of its total surface area. Find the radius & height of the cylinder.

→ Here, given that

The total surface area of solid cylinder = 462 cm²

And given that,

$$\left. \begin{array}{l} \text{Curved surface area} \\ \text{of solid cylinder} \end{array} \right\} = \frac{1}{3} \left(\text{Total surface area of solid cylinder} \right)$$

$$\Rightarrow 2\pi r h = \frac{1}{3} (462)$$

$$2\pi r h = 154$$

$$\boxed{h = \frac{49}{2r}}$$

$$\text{Again, Total surface area of Solid Cylinder } \left. \right\} = 2\pi r(h+r)$$

$$2\pi r(h+r) = 462$$

$$2\pi r\left(\frac{49}{2r} + r\right) = 462$$

$$49 + 2r^2 = 147$$

$$2r^2 = 98$$

$$\boxed{r = 7 \text{ cm}}$$

$$\Rightarrow h = \frac{49}{2r} = \frac{49}{2(7)} = \frac{7}{2} = 3.5 \text{ cm}$$

Thus, the height of required solid cylinder = 3.5 cm

The radius of required solid cylinder = 7 cm

7) Find the ratio between the total surface area of a cylinder to its curved surface area, given that height & radius of the tank are 7.5 m & 3.5 m.

→ Given that,

Height of the cylinder = 7.5 m = (h)

Radius of the cylinder = 3.5 m = (r)

We know that,

Total surface area of cylinder = $2\pi r(h+r)$

Curved surface area of cylinder = $2\pi rh$

$$\text{Then, } \frac{\text{TSA of cylinder}}{\text{CSA of cylinder}} = \frac{2\pi r(h+r)}{2\pi rh}$$

$$= \frac{(h+r)}{h}$$

$$= 1 + \frac{r}{h}$$

$$= 1 + \frac{3.5}{7.5}$$

$$= \frac{22}{15}$$

$$\boxed{\text{TSA : CSA} = 22 : 15}$$

Thus, the ratio between total surface area of a cylinder to its curved surface area is found to be 22:15.

Exercise 19.2

1.) A soft drink is available in two packs.

i) a tin can with a rectangular base of length 5 cm & width 4 cm, having a height of 15 cm and

ii) a plastic cylinder with circular base of diameter 7 cm and height 10 cm, which container has greater capacity & by how much?

→ (i) Given that,

Length of can (l) = 5 cm

Breadth of can (b) = 4 cm

Height of can (h) = 15 cm

Then, Capacity of can = Volume of tin can = $l \times b \times h$
 $= 5 \times 4 \times 15$

$$\boxed{\text{Capacity of can} = 300 \text{ cm}^3} \quad \text{--- ①}$$

(ii) Given that,

Base diameter of cylinder = 7 cm

\Rightarrow Radius of base of cylinder = $r = 3.5$ cm

Height of cylinder (h) = 10 cm

Then, Capacity of cylinder = Volume of cylinder

$$= \pi r^2 h$$

$$= \frac{22}{7} (3.5)^2 \times 10$$

$$\boxed{\text{Capacity of cylinder} = 385 \text{ cm}^3} \quad \text{--- ②}$$

Now, from ① & ② we can say that, the capacity of cylinder is greater than capacity of can.

Hence, the difference in } = (385 - 300) = 85 \text{ cm}^3

2.) The pillars of a temple are cylindrically shaped. If each pillar has a circular base of radius 20cm and height 10m. How much concrete mixture would be required to build 14 such pillars?

→ Here, given that
The pillars of a temple are cylindrically shaped.

The base radius of circular
base of a pillar } = $r = 20\text{cm}$

Height of pillar (h) = $10\text{m} = 1000\text{cm}$

Then, the concrete mixture required to build such pillars is nothing but the volume of the cylindrical pillar.

$$\Rightarrow \text{Volume of pillar} = \pi r^2 h \\ = \left(\frac{22}{7}\right) (20)^2 (1000)$$

$$\boxed{\text{Volume of pillar} = 8.87 \text{ m}^3}$$

Thus, to make one pillar amount of concrete needed is 8.87 m^3 ,

Now, to make such 14 pillars, the amount of concrete needed is = 14×8.87
 $= 124.18 \text{ m}^3$

3.) The inner diameter of a cylindrical wooden pipe is 24cm & its outer diameter is 28cm. The length of the pipe is 35cm. Find the mass of the pipe, if 1 cm^3 of wood has mass of 0.6gm,

→ Let us consider R_1 is the inner radius of cylindrical wooden pipe & R_2 is the outer radius.

From given condition,

$$R_1 = \frac{24}{2} = 12\text{cm} \quad \& \quad R_2 = \frac{28}{2} = 14\text{cm}$$

Length of pipe (l) = 35cm

We know that, $\text{Volume} = \frac{\text{Mass}}{\text{density}}$

$$\begin{aligned} \text{Then, mass of pipe} &= \text{volume} \times \text{density} \\ &= \pi (R^2 - r^2) h \\ &= \frac{22}{7} (14^2 - 12^2) 35 \end{aligned}$$

$$\boxed{\text{Mass of pipe} = 5720 \text{ cm}^3}$$

Given that, mass of 1 cm^3 of wood = 0.6 gm

$$\begin{aligned} \text{Then, total mass of pipe of } 5720 \text{ cm}^3 &= 5720 \times 0.6 \\ &= 3432 \text{ gm} \\ &= 3.432 \text{ kg} \end{aligned}$$

4.) If the lateral surface of a cylinder is 94.2 cm^2 and its height is 5 cm , find i) Radius of its base
ii) Volume of the cylinder

→ Here, given that $(\pi = 3.141)$

$$\text{Lateral surface area of cylinder} = 94.2 \text{ cm}^2$$

$$\text{Height of cylinder (h)} = 5 \text{ cm}$$

Let us consider, 'r' is the base radius of cylinder.

$$\text{Then, (i) Lateral surface area of cylinder} = 2\pi rh$$

$$94.2 = 2 \times 3.14 \times r \times 5$$

$$\boxed{r = 3 \text{ cm}}$$

Radius of base of cylinder is found to be 3 cm .

$$\begin{aligned} \text{(ii) Volume of the cylinder} &= \pi r^2 h \\ &= 3.14 \times 3^2 \times 5 \\ &= 141.3 \text{ cm}^3 \end{aligned}$$

Thus, the volume of the cylinder is found to be 141.3 cm^3

5.) The capacity of a closed cylindrical vessel of height 1 m is 15.4 liters. How many square meters of the metal sheet would be needed to make it?

→

Here, given that

$$\begin{aligned} \text{The capacity of cylinder} &= \text{Volume of cylinder} = 15.4 \text{ liters} \\ &= 0.0154 \text{ m}^3 \end{aligned}$$

$$\text{Height of cylinder (h)} = 1 \text{ m}$$

Let 'r' be the radius of cylindrical vessel,

$$\begin{aligned} \text{Then, Volume of cylinder} &= \pi r^2 h \\ 0.0154 &= 3.14 \times r^2 \times 1 \end{aligned}$$

$$\boxed{r = 0.07 \text{ m}}$$

Again

$$\begin{aligned} \text{Total surface area of vessel} &= 2\pi r(r+h) \\ &= 2 \times 3.14 \times (0.07) \times \\ &\quad (0.07+1) \\ &= 0.470 \text{ m}^2 \end{aligned}$$

Thus, the metal sheet needed to make the cylindrical vessel is found to be 0.470 m^2 .

6) A patient in a hospital is given soup daily in a cylindrical bowl of diameter 7 cm. If the bowl is filled with soup to a height of 4 cm, how much soup the hospital has to prepare daily to serve 250 patients?

→ Given that,

$$\text{Diameter of cylindrical bowl} = 7 \text{ cm}$$

$$\text{Then, Radius of cylindrical bowl} = r = 3.5 \text{ cm}$$

$$\text{Height of the soup filled in a bowl} = h = 4 \text{ cm}$$

$$\begin{aligned} \text{Then, Volume of bowl} &= \pi r^2 h \\ &= \frac{22}{7} \times (3.5)^2 \times 4 \\ &= 154 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Then, the volume of soup in 250 bowls} &= 250 \times 154 \\ &= 38500 \text{ cm}^3 \\ &= 38.5 \text{ liters} \end{aligned}$$

Thus, hospital has to prepare daily 38.5 liters of soup to serve 250 patients.

7) A hollow garden roller, 63cm wide with a girth of 440cm, is made of 4cm thick iron. Find the volume of the iron.

→ Here, given that

Thickness of roller = 4cm

Height of roller (h) = 63cm

The circumference of outer part of roller = 440cm

Let us consider, R_1 is the outer radius and R_2 is the inner radius of roller.

Then, Circumference = $2\pi R_1$

$$440 = 2 \times \frac{22}{7} \times R_1$$

$$\boxed{R_1 = 70 \text{ cm}}$$

Inner Radius (R_2) = $R_1 - 4$

$$R_2 = 70 - 4$$

$$\boxed{R_2 = 66 \text{ cm}}$$

Then, Volume of the iron = $\pi (R_1^2 - R_2^2) h$

$$= \frac{22}{7} (70^2 - 66^2) 63$$

$$= 107712 \text{ cm}^3$$

Thus, the required volume of the iron is 107712 cm^3 .

g.) The cost of painting the total outside surface of a closed cylindrical oil tank at 50 paise per square decimeters is Rs. 198. The height of the tank is 6 times the radius of the base of the tank. Find the volume of the corrected to 2 decimal places.

→ Here, given that

Height of cylindrical tank = 6 (Radius of base tank)

$$\boxed{h = 6r}$$

Let 'r' be the radius of base of tank.

Also, The cost of painting per square decimeter is Rs. 198.

$$\Rightarrow 2\pi r(r+h) \times \frac{1}{2} = 198$$

$$2 \left(\frac{22}{7}\right) (r) (r+r) \times \frac{1}{2} = 198$$

$$\boxed{r = 3 \text{ dm}}$$

$$h = 6r = 6 \times 3 = 18 \text{ dm}$$

Now, Volume of cylindrical tank = $\pi r^2 h$

$$= \frac{22}{7} (3) (18)$$

$$= 509.14 \text{ dm}^3$$

Thus, the volume of the cylindrical tank is found to be 509.14 dm^3 .

10.) The radii of two cylinders are in the ratio 2:3 and their heights are in the ratio 5:3. Calculate the ratio of their volumes & the ratio of their curved surfaces.

→ Given that,

The radii of two cylinders are in the ratio 2:3.

The heights of two cylinders are in the ratio 5:3.

Then, $2x$ and $3x$ be radii of two cylinders respectively and $5y$ & $3y$ be the heights of two cylinders respectively.

$$\text{Now, } \frac{(\text{Volume of cylinder 1})}{(\text{Volume of cylinder 2})} = \frac{\pi (2x)^2 5y}{\pi (3x)^2 3y} = \frac{20}{27}$$

$$\text{And } \frac{(\text{Surface area of cylinder 1})}{(\text{Surface area of cylinder 2})} = \frac{2\pi (2x) 5y}{2\pi (3x) 3y} = \frac{10}{9}$$

11.) The ratio between the curved surface area & the total surface area of right circular cylinder is 1:2. Find the volume of the cylinder, if its total surface area is 616 cm^2 .

→ Here, given that

$$\text{Total surface area of RCC} = 616 \text{ cm}^2$$

Let 'h' be the height of cylinder and
'r' be the radius of cylinder.

From given condition,

$$\frac{\text{Curved Surface Area}}{\text{Total Surface Area}} = \frac{1}{2}$$

$$\Rightarrow \text{CSA} = \frac{1}{2} (\text{TSA})$$

$$\text{CSA} = \frac{1}{2} (616) = 308 \text{ cm}^2$$

$$\boxed{\text{CSA} = 308 \text{ cm}^2}$$

Now, $\text{Total Surface Area} = 2\pi rh + 2\pi r^2$

$$616 = \text{CSA} + 2\pi r^2$$

$$616 = 308 + 2\pi r^2$$

$$2\pi r^2 = 616 - 308$$

$$2\pi r^2 = 308$$

$$r^2 = 308 / 2\pi$$

$$r^2 = 49$$

$$\boxed{r = 7 \text{ cm}}$$

Now, $\text{CSA} = 308 \text{ cm}^2$

$$2\pi rh = 308$$

$$2 \left(\frac{22}{7}\right) \times 7 \times h = 308$$

$$\boxed{h = 7 \text{ cm}}$$

Then, $\text{Volume of Cylinder} = \pi r^2 h$
 $= \frac{22}{7} (7)^2 (7)$
 $= 1078 \text{ cm}^3$

Thus, the volume of cylinder is found to be 1078 cm^3 .

12.) The curved surface area of a cylinder is 1320 cm^2 and its base had diameter 21 cm . Find the height & volume of the cylinder.

→ Here given that,

$$\text{Curved surface area of a cylinder} = 1320 \text{ cm}^2$$

$$\text{The base diameter of a cylinder} = 21 \text{ cm}$$

$$\text{Then, base radius of a cylinder } (r) = 10.5 \text{ cm}$$

We have,

$$\text{Curved surface area of a cylinder} = 2\pi r h$$

$$1320 = 2 \times \frac{22}{7} \times 10.5 \times h$$

$$\boxed{h = 20 \text{ cm}}$$

$$\begin{aligned} \text{Now, Volume of a cylinder} &= \pi r^2 h \\ &= \frac{22}{7} \times (10.5)^2 \times 20 \end{aligned}$$

$$= 6930$$

Thus, the volume of a cylinder is found to be 6930 cm^3 .

13.) The ratio between the radius of the base & the height of a cylinder is $2:3$. Find the total surface area of the cylinder, if its volume is 1617 cm^3 .

→ Let us first consider that

r - be the radius of base of cylinder and

h - be the height of a cylinder

Here, given that $r:h = 2:3$

If radius $= 2x$ then height $= 3x$

We know that, Volume of cylinder $= \pi r^2 h$

$$1617 = \frac{22}{7} (2x)^2 (3x)$$

$$1617 = \frac{22}{7} (12x^3)$$

$$x^3 = 343/8$$

$$x = 7/2$$

$$\boxed{x = 3.5 \text{ cm}}$$

Then, Radius of cylinder (r) = $2x = 2(3.5) = 7\text{cm}$
Height of cylinder (h) = $3x = 3(3.5) = 10.5\text{cm}$

But, The total surface area of a cylinder } = $2\pi r(h+r)$
= $2\left(\frac{22}{7}\right)(7)(10.5+7)$
= 770 cm^2

Thus, the total surface area of a cylinder is found to be 770 cm^2 .

14.) A rectangular sheet of paper, $44\text{cm} \times 20\text{cm}$, is rolled along its length to form a cylinder. Find the volume of the cylinder so formed.

→ Here, given that

Length of rectangular sheet = 44cm (l)

Breadth of rectangular sheet = 20cm (b)

from given condition, we can write

$$2\pi r = 44$$

$$r = 44/2\pi$$

$$\boxed{r = 7\text{cm}}$$

But, Volume of a cylinder = $\pi r^2 h$
= $\frac{22}{7}(7)^2(20)$
= 3080 cm^3

Thus, the volume of a cylinder is found to be 3080 cm^3 .

15.) The curved surface area of a cylindrical pillar is 264 m^2 and its volume is 924 m^3 . Find the diameter and the height of the pillar?

→

②

Let us consider 'r' is the radius of cylindrical pillar and 'h' is the height of cylindrical pillar.

Given that, Curved surface area of cylindrical pillar } = 264 m²

Now, $2\pi rh = 264$

$$\pi rh = 132 \quad \text{--- (1)}$$

But, Volume of the cylinder = 924 m³

$$\pi r^2 h = 924$$

$$(\pi rh) r = 924 \quad \text{by (1)}$$

$$(132)r = 924$$

$$r = 924/132$$

$$\boxed{r = 7\text{m}}$$

Thus, $\pi rh = 132$

$$\pi (7)h = 132$$

$$\boxed{h = 6\text{m}}$$

Thus, diameter of the pillar = $2r = 2(7) = 14\text{m}$
Height of the pillar = 6m

16.) Write the no. of surfaces of a right circular cylinder.

→ There are total 3 surfaces in a right circular cylinder.

17.) Write the ratio of total surface area to the curved surface area of a cylinder of radius r & height h.

$$\rightarrow \frac{\text{Total Surface area of cylinder}}{\text{Curved Surface area of cylinder}} = \frac{2\pi r(h+r)}{2\pi rh} = \frac{h+r}{h}$$