

Cubes and Cube Roots

Exercise 7.1

(1) Which of the following number are not perfect cubes?

(i) 216

Ans: Here, we find cube root of given number.

2	216
2	108
2	54
3	27
3	9
3	3
	1

By prime factorization

$$216 = \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3}$$

We make group of 3 factor.

$$216 = 2^3 \times 3^3$$

$$= (2 \times 3)^3$$

$$= 6^3 \text{ which is perfect cube.}$$

216 is a perfect cube of 6.

(ii) 128

Ans: Here, we find cube root of given number.

$$\begin{array}{r|l}
 2 & 128 \\
 \hline
 2 & 64 \\
 \hline
 2 & 32 \\
 \hline
 2 & 16 \\
 \hline
 2 & 8 \\
 \hline
 2 & 4 \\
 \hline
 & 2
 \end{array}$$

$$128 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times 2$$

We make group of 3 factor.

In above factorization one triplet group of 2 is not form.

128 is not a perfect cube.

(iii) 1000

ANS:

$$\begin{array}{r|l}
 2 & 1000 \\
 \hline
 2 & 500 \\
 \hline
 2 & 250 \\
 \hline
 5 & 125 \\
 \hline
 5 & 25 \\
 \hline
 5 & 5 \\
 \hline
 & 1
 \end{array}$$

We make group of 3 factor.

$$1000 = \underline{5 \times 5 \times 5} \times \underline{2 \times 2 \times 2}$$

We make group of 3 factor.

$$1000 = 2^3 \times 5^3$$

$$= (5 \times 2)^3$$

= 10^3 which is a perfect cube

1000 is a perfect cube of 10.

(iv) 100

ANS:

$$\begin{array}{r|l} 2 & 100 \\ \hline 2 & 50 \\ \hline 5 & 25 \\ \hline 5 & 5 \\ \hline & 1 \end{array}$$

By prime factorization

$$100 = 5 \times 5 \times 2 \times 2$$

Here each factor repeated only twice. We required 3 times.

100 is not a perfect cube.

(v) 46656

ANS:

$$\begin{array}{r|l} 2 & 46656 \\ \hline 2 & 23328 \\ \hline 2 & 11664 \\ \hline 2 & 5832 \\ \hline 2 & 2916 \\ \hline 2 & 1458 \\ \hline 3 & 729 \\ \hline 3 & 243 \\ \hline 3 & 81 \\ \hline 3 & 27 \\ \hline 3 & 9 \\ \hline & 3 \end{array}$$

By prime factorization

We make group of 3 factor.

$$46656 = \underline{3 \times 3 \times 3} \times \underline{3 \times 3 \times 3} \times \underline{4 \times 4 \times 4}$$

Here each factor appear 3 time

$$46656 = 3^3 \times 3^3 \times 4^3$$

$$= (3 \times 3 \times 4)^3$$

$$= (36)^3 \text{ which is a perfect cube.}$$

46656 is a perfect cube of 36.

(2) Find the smallest number by which each of the following number must be multiplied to obtain a perfect cube.

ANS:

By using smallest multiple method,

$$\begin{array}{r|l}
 3 & 243 \\
 \hline
 3 & 81 \\
 \hline
 3 & 27 \\
 \hline
 3 & 9 \\
 \hline
 & 3
 \end{array}$$

$$243 = \underline{3 \times 3 \times 3} \times 3 \times 3$$

Here, the prime factor 3 does not appear in a group of three.

For getting a perfect cube, we multiply by one more 3.

$$243 \times 3 = \underline{3 \times 3 \times 3} \times \underline{3 \times 3 \times 3}$$

$$= 729 \text{ which is a perfect cube.}$$

The smallest natural number by which 243 should be multiplied to make a perfect cube is 3.

(ii) 256

ANS:

$$\begin{array}{r|l}
 2 & 256 \\
 \hline
 2 & 128 \\
 \hline
 2 & 64 \\
 \hline
 2 & 32 \\
 \hline
 2 & 16 \\
 \hline
 2 & 8 \\
 \hline
 2 & 4 \\
 \hline
 2 & 2 \\
 \hline
 & 1
 \end{array}$$

Here,

$$256 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2}$$

The prime factor 2 does not appear in a group of three.

For getting a perfect cube, we multiply by one more 2.

$$256 \times 2 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2}$$

= 512 which is a perfect cube.

The smallest natural number by which 256 should be multiplied to make perfect cube is 2.

(iii) 72

ANS:

$$\begin{array}{r|l}
 2 & 72 \\
 \hline
 2 & 36 \\
 \hline
 2 & 18 \\
 \hline
 3 & 9 \\
 \hline
 3 & 3 \\
 \hline
 & 1
 \end{array}$$

$$72 = 2 \times 2 \times 2 \times 3 \times 3$$

Here,

The prime factor 3 does not appear in a group of three.

For getting a perfect cube, we multiply by one more 3.

$$72 \times 3 = \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3}$$

= 216 which is a perfect cube.

The smallest natural number by which 72 should be multiplied to make a perfect cube is 3.

(iv) 675

ANS:

$$\begin{array}{r|l} 5 & 675 \\ \hline 5 & 135 \\ \hline 3 & 27 \\ \hline 3 & 9 \\ \hline 3 & 3 \end{array}$$

$$675 = \underline{3 \times 3 \times 3} \times 5 \times 5$$

Here,

The prime factor 5 does not appear in a group of three.

For getting a perfect cube, we multiply by one more 5.

$$675 \times 5 = \underline{3 \times 3 \times 3} \times \underline{5 \times 5 \times 5}$$

= 3375 which is a perfect cube.

The smallest natural number by which 675 should be multiplied to make a perfect cube is 5.

(v) 100

ANS:

2	100
2	50
5	25
5	5
	1

$$100 = 5 \times 5 \times 2 \times 2$$

Here both the prime factor does not form a group of three.

For getting a perfect cube, we multiply by 5 and 2

$$\text{Then, } 100 \times 5 \times 2 = \underline{5 \times 5 \times 5} \times \underline{2 \times 2 \times 2}$$

= 1000 which is a perfect cube.

The smallest natural number by which 100 should be multiplied to make a perfect cube is 5 x 2

(3) Find the smallest number by which each of the following number must be divided to obtain a perfect cube.

(i) 81

ANS:

3	81
3	27
3	9
3	3
	1

$$81 = \underline{3 \times 3 \times 3} \times 3$$

Factor 3 does not form a group of three.

If we divide 81 by 3, then the prime factorization of the quotient will not contain 3.

$$81 \div 3 = 3 \times 3 \times 3$$

= 27 = 3³ is perfect cube.

The smallest number by which 81 should be divided to make it perfect cube is 3.

(ii) 128

ANS:

$$\begin{array}{r|l} 2 & 128 \\ \hline 2 & 64 \\ \hline 2 & 32 \\ \hline 2 & 16 \\ \hline 2 & 8 \\ \hline 2 & 4 \\ \hline 2 & 2 \\ \hline & 1 \end{array}$$

$$128 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times 2$$

Factor 2 does not form a group of three,

if we divide 128 by 2, then the prime factorization of the quotients will not contain 2.

$$128 \div 2 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2}$$

$$= 64 = 4^3 \text{ is perfect cube.}$$

The smallest number by which 128 should be divided to make it perfect cube is 2.

(iii) 135

ANS:

$$\begin{array}{r|l} 5 & 135 \\ \hline 3 & 27 \\ \hline 3 & 9 \\ \hline 3 & 3 \end{array}$$

$$135 = \underline{3 \times 3 \times 3} \times 5$$

Factor 5 does not form a group of three

If we divide 135 by 5, then the prime factorization of the quotient will not contain 5.

$$135 \div 5 = 3 \times 3 \times 3$$

$= 27 = 3^3$ is perfect cube.

The smallest number by which 135 should be divided to make it perfect cube is 5.

(iv) 192

ANS:

$$\begin{array}{r|l} 2 & 192 \\ \hline 2 & 96 \\ \hline 2 & 48 \\ \hline 2 & 24 \\ \hline 2 & 12 \\ \hline 2 & 6 \\ \hline 3 & 3 \\ \hline & 1 \end{array}$$

$$192 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times 3$$

Factor 3 does not form a group of three

If we divide 192 by 3 then the prime factorization of the quotient will not contain 3.

$$192 \div 3 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2}$$

$= 64 = 4^3$ is perfect cube.

The smallest number by which 192 should be divided to make it perfect cube is 3.

(v) 704

ANS:

2	704
2	352
2	176
2	88
2	44
2	22
	11

$$704 = \underline{2} \times \underline{2} \times \underline{2} \times \underline{2} \times \underline{2} \times \underline{2} \times 11$$

Factor 11 does not form a group of three

If we divide 704 by 11 then the prime factorization of the quotient will not contain 11.

$$704 \div 11 = \underline{2} \times \underline{2} \times \underline{2} \times \underline{2} \times \underline{2} \times \underline{2}$$

= 64 = 4³ is perfect cube.

The smallest number by which 704 should be divided to make it perfect cube is 11.

(4) Parikshit makes a cuboid of plasticine of sides 5cm, 2cm, 5cm, how many such cuboids will he need to form a cube?

ANS:

Given that,

Parikshit have plasticine of sides 5cm, 2cm and 5cm

We know,

Number of cuboids required = Volume of cube / Volume of cuboid

Now, Volume of cuboid = length x breadth x height

$$\text{Volume of cuboid} = 5 \times 5 \times 2 \text{ cm}^3$$

To make the volume of cuboid as a cube number we need to multiply it by (5 x 2 x 2)

$$\text{Number of cuboids required} = \frac{5^3 \times 2^3}{5^2 \times 2}$$

$$\text{Number of cuboids required} = 20$$

Exercise 1.2

(1) Find the cube root of each of the following numbers by prime factories method.

(i) 64

ANS:

By prime factor method,

$$\begin{array}{r|l} 2 & 64 \\ \hline 2 & 32 \\ \hline 2 & 16 \\ \hline 2 & 8 \\ \hline 2 & 4 \\ \hline 2 & 2 \\ \hline & 1 \end{array}$$

$$64 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2}$$

We make group of 3 factor.

$$= 2^3 \times 2^3$$

$$= (2 \times 2)^3$$

The cube root of 64 is 4

(ii) 512

ANS:

By prime factor method

2	512
2	256
2	128
2	64
2	32
2	16
2	8
2	4
2	2

$$512 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2}$$

We make group of 3 factor.

$$= 2^3 \times 4^3$$

$$= (2 \times 2 \times 2)^3$$

The cube root of 512 is 8.

(iii) 10648

ANS:

By prime factor method

2	10648
2	5324
2	2662
11	1331
11	121
11	11
	1

We make group of 3 factor.

$$10648 = \underline{2 \times 2 \times 2} \times \underline{11 \times 11 \times 11}$$

$$= 2^3 \times 11^3$$

$$= (2 \times 11)^3$$

The cube root of 10648 is 22

(iv) 27000

ANS:

By prime factor method,

$$\begin{array}{r|l} 3 & 27000 \\ \hline 3 & 9000 \\ \hline 3 & 3000 \\ \hline 10 & 1000 \\ \hline 10 & 100 \\ \hline 10 & 10 \\ \hline & 1 \end{array}$$

We make group of 3 factor.

$$27000 = \underline{3 \times 3 \times 3} \times \underline{10 \times 10 \times 10}$$

$$= 3^3 \times 10^3$$

$$= (3 \times 10)^3$$

The cube root of 27000 is 30.

(v) 15625

ANS:

By prime factor method,

$$\begin{array}{r|l}
 5 & 15625 \\
 \hline
 5 & 3125 \\
 \hline
 5 & 625 \\
 \hline
 5 & 125 \\
 \hline
 5 & 25 \\
 \hline
 5 & 5 \\
 \hline
 & 1
 \end{array}$$

We make group of 3 factor.

$$15625 = \underline{5 \times 5 \times 5} \times \underline{5 \times 5 \times 5}$$

$$= 5^3 \times 5^3$$

$$= (5 \times 5)^3$$

The cube root of 15625 is 25.

(vi) 13824

ANS:

By prime factor method

2	13824
2	6912
2	3456
2	1728
2	864
2	432
2	216
2	108
2	54
3	27
3	9
3	3
	1

We make group of 3 factor.

$$13824 = \underline{2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3}$$

$$= 2^3 \times 2^3 \times 2^3 \times 3^3$$

$$= (2 \times 2 \times 2 \times 3)^3$$

The cube root of 13824 is 24.

(vii) 110592

ANS:

By prime factorization method,

2	110592
2	55296
2	27648

2	13824
2	6912
2	3456
2	1728
2	864
2	432
2	216
2	108
2	54
3	27
3	9
3	3
	1

We make group of 3 factor.

$$\begin{aligned}
 110592 &= \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3} \\
 &= 2^3 \times 2^3 \times 2^3 \times 2^3 \times 3^3 \\
 &= (2 \times 2 \times 2 \times 2 \times 3)^3
 \end{aligned}$$

The cube root of 110592 is 48.

(viii) 46656

ANS:

By prime factorization method

2	46656
2	23328
2	11664
2	5832
2	2916
2	1458
3	729
3	243
3	81
3	27
3	9
3	3
	1

We make group of 3 factor.

$$46656 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{3 \times 3 \times 3} \times \underline{3 \times 3 \times 3}$$

$$= 2^3 \times 2^3 \times 3^3 \times 3^3$$

$$= (2 \times 2 \times 3 \times 3)^3$$

The cube root of 46656 is 36.

(ix) 175616

ANS:

By prime factorization method

2	175616
2	87808
2	43904
2	21952
2	10976
2	5488
2	2744
2	1372
2	686
7	343
7	49
7	7
	1

We make group of 3 factor.

$$175616 = \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{2 \times 2 \times 2} \times \underline{7 \times 7 \times 7}$$

$$175616 = 2^3 \times 2^3 \times 2^3 \times 7^3$$

$$= (2 \times 2 \times 2 \times 7)^3$$

The cube root of 175616 is 56.

(x) 91125

ANS:

By prime factorization method,

5	91125
5	18225
5	3645
3	729
3	243
3	81
3	27
3	9
3	3

We make group of 3 factor.

$$\begin{aligned}
 91125 &= \underline{5 \times 5 \times 5 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3} \\
 &= 5^3 \times 3^3 \times 3^3 \\
 &= (5 \times 3 \times 3)^3
 \end{aligned}$$

The cube root of 91125 is 45.

(2) State true or false

(i) Cube of any odd number is even.

ANS:False.

(ii) A perfect cube does not end with two zero.

ANS:True.

(iii) If square of a number end with 5, then its cube end with 25.

ANS:False.

(iv) There is no perfect cube which ends with 8.

ANS:False.

(v) The cube of a two digit number may be three digit numbers.

Answer: False.

(vi) The cube of a two digit number may have seven or more digits.

ANS:False.

(vii) The cube of a single digit number may be a single digit number.

ANS:True.